

# The Discontinuous Galerkin Method on Heterogeneous Architectures

**Malcolm Roberts**, IRMA, Université de Strasbourg

**Philippe Helluy**, IRMA, Université de Strasbourg

**Bruno Weber**, IRMA, Université de Strasbourg

**Emmanuel Franck**, IRMA, Université de Strasbourg

The discontinuous Galerkin (DG) method is a highly adaptable method which can be used to solve systems of hyperbolic conservation laws in complex geometries[1]. While the DG method has various useful properties, it is also computationally intensive and difficult to implement. To deal with the computational complexity, we have used the `OpenCL` programming environment, allowing us to run on CPUs, GPUs, and MICs; one can implement an algorithm in an `OpenCL` kernel which is compiled at run-time for each device on which the algorithm is to be run. Moreover, one can make use of, for example, the CPU and GPU in parallel. However, memory management and load balancing can quickly become cumbersome, requiring much tedious programming work. We make use of the `StarPU`[3] runtime environment to deal with these issues. Here we present the `schnaps`[2] DG implementation, where the spatial domain is divided into macrocells of constant curvature which are represented as individual contiguous arrays in the computer's memory. By maintaining a constant curvature in each macrocell, we simplify the geometrical terms in the flux computation, and by separating the macrocell memory buffers, we have a natural parallelism between macrocells which can in principle be used by `StarPU` to divide the work between compute devices.

## Références

- [1] G. COHEN, X. FERRIERES, AND S. PERNET, *A spatial high-order hexahedral discontinuous galerkin method to solve maxwells equations in time domain*, J. Comput. Phys., 217(2):340363, 2006.
- [2] `schnaps.gforge.inria.fr`
- [3] `starpup.gforge.inria.fr`

**Malcolm Roberts**, IRMA, 7 rue Ren-Descartes, 67084 Strasbourg  
`malcolmiwroberts@gmail.com`

**Philippe Helluy**, IRMA, 7 rue Ren-Descartes, 67084 Strasbourg  
`helluy@math.unistra.fr`

**Bruno Weber**, IRMA, 7 rue Ren-Descartes, 67084 Strasbourg  
`bruno.weber@axessim.fr`

**Emmanuel Franck**, IRMA, 7 rue Ren-Descartes, 67084 Strasbourg  
`emmanuel.franck@inria.fr`